Effect of heterogeneous APD restitution on VF organization in a model of the human ventricles

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Abstract

The onset of ventricular fibrillation (VF) has been associated with steep action potential duration (APD) restitution in both clinical and computational studies. Recently, detailed clinical restitution properties in cardiac patients were reported showing a substantial degree of heterogeneity in restitution slopes at the epicardium of the ventricles. The aim of the present study was to investigate the effect of heterogeneous restitution properties in a 3D model of the ventricles using these clinically measured restitution data. We used a realistic model of the human ventricles, including detailed descriptions of cell electrophysiology, ventricular anatomy, and fiber direction anisotropy. We extended this model by mapping the clinically observed epicardial restitution data to our anatomical representation using a diffusion based algorithm. Restitution properties were then fitted by regionally varying parameters of the electrophysiological model. We studied the effects of restitution heterogeneity on the organization of VF by analyzing filaments and the distributions of excitation periods. We found that the number of filaments and the excitation periods were both dependent on the extent of heterogeneity. An increased level of heterogeneity leads to a greater number of filaments and a broader distribution of excitation periods, thereby increasing the complexity and dynamics of VF. Restitution heterogeneity may play an important role in providing a substrate for cardiac arrhythmias.

Introduction

Sudden cardiac death is the most common cause of death in the industrialized world and in most cases it is due to ventricular fibrillation (VF) [59]. During VF, excitation waves are disturbed and chaotic, causing the contraction of the ventricles to become rapid and uncoordinated. It has been shown in clinical and experimental studies that these turbulent wave patterns are underpinned by re-entrant sources of excitation [12, 15, 54, 28, 19, 51]. If VF is not halted by means of defibrillation, this condition can be lethal within minutes.

Historically, it has been hypothesized that VF is due to turbulent wave propagation induced by heterogeneity in refractoriness of cardiac tissue [27, 23]. The important role of heterogeneity in VF is supported by the strong association of VF with diseases that lead to increased heterogeneity, such as coronary artery disease, cardiomyopathies, and congenital heart disease [59, 11]. Due to these pathologies, remodeling of the cellular ionic currents, calcium handling and gap junctional coupling in cardiac tissue results in increased heterogeneity. Furthermore, VF is associated with diseases such as Long QT, Short QT, and Brugada syndrome [59, 11], in which ion channel mutations lead to an increase of action potential duration (APD) dispersion.

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In the last decade, it has been proposed that VF is caused by the occurrence of dynamical instabilities (alternans) induced by steep APD restitution [33, 16, 35, 52, 41, 36], which became known as the restitution hypothesis of VF [52, 41]. More recently, intracellular calcium cycling has been shown to cause alternans in APD [53, 40], which may lead to dynamical instabilities and VF. According to the original restitution hypothesis, alternans instability occurs when the slope of the APD restitution curve, which relates the APD to its previous diastolic interval (DI), exceeds one [33, 16]. Recent experimental and modeling studies show that although steepness of restitution curve is an important determinant of instability [3, 2, 55], other factors such as electrotonic coupling, cardiac memory, and conduction velocity restitution should also be taken into account [13, 50, 49, 39]. The restitution hypothesis and refractoriness hypothesis of VF are related. Alternans instability induces dynamic heterogeneities that can lead to wave break, whereas static anatomically defined heterogeneities can also lead to wave break. Restitution induced VF has been the subject of a variety of computational studies. Because the restitution hypothesis does not require pre-existing heterogeneity for the onset of VF, most of the computational studies regarding the restitution hypothesis have assumed that cardiac tissue is homogeneous. However, recent clinical studies have demonstrated that APD restitution properties on the ventricular epicardium and endocardium have a complex spatially non-uniform distribution [58, 31, 26]. These studies showed that: 1) APD restitution properties are spatially heterogeneous containing multiple sites of steep and shallow restitution slopes; 2) Maximum restitution slopes range from almost zero to well over two; 3) Restitution properties differ between patients and are dependent on the underlying pathology. Some studies on the effects of heterogeneous APD restitution in cardiac tissue have shown that spatial dispersion in APD restitution may result in wavebreak and initiation of VF [6, 9, 57]. However, the influence of restitution heterogeneity on VF dynamics and organization has not yet been investigated. In this paper, we study the effects of heterogeneous APD restitution data measured in clinical studies [31] on VF organization in the human heart. We use our integrative anatomical model of the human ventricles [48], which was recently developed and verified against available clinical data on human VF. The model describes action potential characteristics of human ventricular myocytes [50, 49], combined with an anatomically detailed geometry of the human ventricles that incorporates fiber direction anisotropy [18]. We introduce APD restitution heterogeneity into our model by incorporating clinically measured restitution data from patients who were undergoing surgery for aortic valve replacement as reported in [31]. Clinical restitution curves were mapped and interpolated to our 3D ventricular geometry and reproduced by our cell model using appropriate regional variations of the parameters of the electrophysiological model. We used this human ventricular model to study the effects of spatial heterogeneity of APD restitution on the dynamics of VF and found that the organization of VF became more complex with increased heterogeneity. We have quantified these effects in terms of the number of filaments and the local excitation periods.

Methods

We developed a heterogeneous model of the human ventricles by incorporating clinically measured spatially heterogeneous APD restitution properties [31] into our integrative model of the human ventricles [50, 49, 48]. Below we describe in detail the main features of our heterogeneous model.

Ventricular model

Excitation of the ventricles in a monodomain model can be described using the following partial differential Equation [22]:

$$C_m \frac{\partial V_m}{\partial t} = \frac{\partial}{\partial x_j} \left( D_{ij} \frac{\partial V_m}{\partial x_j} \right) - I_{ion}$$

(1)

where $V_m$ denotes the transmembrane voltage, $C_m$ the membrane capacitance, $D_{ij}$ the diffusion tensor, and $I_{ion}$ the sum of the ionic transmembrane currents describing the excitable behavior of the individual ventricular cell. There are different models available to describe action potential characteristics of the cell membrane [4, 24, 25, 1, 13, 50]. In this study, we used the human ventricular ionic model.
published by Ten Tusscher et al. [50, 49] and refer to this as the TNNP model. This model provides a
detailed description of voltage, ionic currents and intracellular ion concentrations, and is based on a wide
range of human based electrophysiological data. The most recent version of the TNNP model [49] includes
a more extensive description of intracellular calcium dynamics. However, the model does not describe
calcium alternans nor spontaneous calcium release. The model reproduces experimentally measured
APD [29] and conduction velocity restitution curves [14]. The TNNP model contains the following ionic
currents:

\[ I_{ion} = I_{Na} + I_{to} + I_{CaL} + I_{Kr} + I_{Ks} + I_{K1} + I_{NaCa} + I_{NaK} + I_{pCa} + I_{pK} + I_{Na,b} + I_{Ca,b} \] (2)

A complete list of all equations can be found in [50, 49]. We used the ‘default’ parameter settings
from [49]; all changes from these default settings are detailed in the text below. More information about
homogeneous 2D and 3D spiral wave dynamics and spiral wave breakup can be found in [49, 48].

Geometric data describing the 3D ventricular anatomy and fiber direction field were derived from
a normal healthy human heart [18]. From this heart, a voxel description of approximately 13.5 million
points with a spatial resolution of 0.25 mm was obtained. We assume that the transverse conductivity is
the same in all directions orthogonal to the direction of the muscle fiber axis and that local conductivity
tensors \( D_{ij} \) can be derived from local muscle fiber directions using:

\[ D_{ij} = D_L \delta_{ij} + (D_L - D_T) \alpha_i \alpha_j \] (3)

where, \( D_L \) and \( D_T \) are the longitudinal and transverse conductivity, respectively and \( \alpha \) is the muscle
fiber direction. For \( D_L \) we used 162 \( \Omega \)cm and for \( D_T \) we used 40.5 \( \Omega \)cm, which resulted in conduction
velocities of 68 cm/s in the longitudinal direction and 32 cm/s in the transverse direction. Thus the
resulting anisotropy ratio was approximately 2:1, which is consistent with clinical measurements [20].

**Clinical human restitution data**

A recent clinical study by Nash et al. [31] has provided global epicardial restitution properties in 14 car-
diatic patients. In this study, activation-recovery intervals (ARI) were recorded over the entire ventricular
epicardial surface using an epicardial sock containing 256 unipolar contact electrodes (inter-electrode
spacing approximately 10 mm). These ARI values can be compared to action potential durations (APD)
measured at approximately 50% repolarization (APD\(_{50}\)) [17]. They applied a standard S1-S2 protocol
to determine restitution properties. A train of 9 S1 stimuli at a basic cycle length (BCL) of 600 ms
were applied, followed by a S2 stimulus at various intervals ranging from 600 ms to 240 ms. For each
electrode, up to 24 pairs of values for the diastolic interval (DI) and subsequent \( APD_{50} \) were recorded.
We fitted the clinical ARI data of Nash et al. [31] using a least-squares mono-exponential fit as this was
the same approach used by Nash et al. [31]:

\[ APD_{50} = APD_{50(SS)} - a \exp(-DI/b) \] (4)

where the steady state \( APD_{50(SS)} \), \( a \) and \( b \) are parameters of the fit. The maximum restitution slope \( S_{max} \) was determined for each electrode using [31]:

\[ S_{max} = (a/b) \exp(-DI_{min}/b) \] (5)

where \( DI_{min} \) is the minimum measured non-refractory DI. Note that this method for maximum
restitution slope determination differs from the method used in Ten Tusscher et al. [49] who used a
piecewise linear approximation to determine the maximum restitution slope. We compared both methods
and found that the piecewise calculation systematically underestimated the maximum restitution slope
by around 0.2-0.3 compared to the least squares mono-exponential fit method (Nash et al. [31]).
Mapping and extrapolating clinical restitution data

In the present study, we used datasets of two patients undergoing replacement surgery for aortic valve disease, for which the most complete APD restitution recordings were available, with more than 85% of valid electrode recordings for each dataset. An electrode was defined to be valid if the data contained at least 18 pairs of DI and \( APD_{50} \) values and the mono-exponential fit had at least a correlation coefficient of 0.6 or higher, with 1 meaning perfect statistical correlation and 0 meaning there is no correlation at all. Maximum restitution slopes (\( S_{\text{max}} \)) with a slope smaller than 0.4 or greater than 3 were manually evaluated and corrected if needed. Dataset 1 (i.e., Figure 4 in [31]) had a mean +/- SD \( S_{\text{max}} \) of 1.78 +/- 1.04, based on \( n = 238 \) (93%) valid restitution curves. For dataset 2, the mean +/- SD \( S_{\text{max}} \) was 0.97 +/- 0.97 based on \( n = 227 \) (89%) valid restitution curves.

To map the clinical restitution data to our human ventricles, we first mapped the positions of the 256 sock electrodes to the surface of our ventricular model. Coordinates of both the epicardial sock and the anatomical model were normalized about the center of the apex taking into account the anterior, posterior, left and right sides of the ventricles. Electrode sites were then projected on the epicardial surface of our ventricular model by minimizing the distance to the epicardial surface.

For our study, we needed to assign restitution properties of cardiac tissue throughout the entire 3D ventricular mass. However, data on the full 3D organization of APD restitution in the human ventricles are presently not available. Observations have been reported only for surfaces of the heart, and measuring restitution properties on the epi- and endocardium require different clinical methods. To date, either epicardial or endocardial recordings (but not both) have been reported for individual hearts. Nash et al. [31] used an epicardial sock with electrodes to measure restitution data at 256 locations spread across most of the epicardium. Yue et al. [58] used a catheter balloon with electrodes to measure restitution data at 128 locations on the endocardium of the heart. The epi- and endocardial data sets each show regional organization of restitution slopes into 3-5 different areas. Slopes varied between regions and the spatial arrangement of these regions varied considerably from patient to patient. Given these observations regarding restitution slope patterns on the epi- and endocardial surfaces, it is likely that this heterogeneity has a 3D structure. In the absence of experimental 3D data, we extrapolated the 2D surface patterns across the 3D mass. Rather than using different data sets from two different hearts (i.e., one set of data for the epicardial surface, and another for the endocardial surface), we used only the epicardial data from Nash et al. [31]. In order to extrapolate the data into 3D, we developed a diffusion based algorithm to extend the epicardial profile smoothly across the ventricular walls (described below). We do not claim that our algorithm will reproduce the quantitatively correct 3D restitution profile for a particular patient. However, we believe that this is a reasonable first step until more detailed data on 3D organization of human restitution becomes available.

Diffusion domain algorithm

Our diffusion algorithm contains the following three steps.

Firstly, we extended the measured \( S_{\text{max}} \) values (maximum 256 electrode points on the epicardium) to all heart points by solving the diffusion equations for the maximum restitution slopes in the domain given by the heart anatomy. We used the clinically measured maximum restitution slopes as constraints, i.e., the variable \( S_{\text{max}} \) was kept constant at each electrode position during the diffusion process. We used a value for the non-dimensional diffusion coefficient of \( D = 400 \), which provided the desired spatial smoothness of interpolation. The diffusion equations were solved until the average square of residual at the non-constraint points decreased below \( 10^{-10} \). As a result, we obtained a smooth spatial interpolation of \( S_{\text{max}} \) across all points in the 3D model except for the regions immediately adjacent to the initial electrodes.

The second step was to remove these sharp local gradients by applying a moving average window of \( 3 \times 3 \times 3 \) voxels in the domain given by the heart anatomy. Note that this averaging also changed the values of \( S_{\text{max}} \) at the reference electrodes (see Figure 1, column 2). As a third step, we scaled back \( S_{\text{max}} \) values for all points using a linear transformation function, which was found from the data presented in Figure 2. More specifically, we found the best least square linear fit of the the original, clinically
measured maximum restitution slope values and the $S_{\text{max}}$ values found after step 2 of our interpolation procedure. We then scaled back our data using this linear transformation. Thus, we obtained a smooth distribution of $S_{\text{max}}$ across all heart points in our anatomical model, which corresponded well with the clinical data at the epicardial surface.

Figure 1 shows the application of our algorithm for dataset 1 (the upper row) and dataset 2 (the lower row). In the first column, we show a direct linear surface interpolation of the clinical data using Matlab’s GRIDDATA function. In the second column, we show how $S_{\text{max}}$ values are distributed after the diffusion algorithm and the $3 \times 3 \times 3$ moving average window were applied. The third column shows the maximum restitution slopes after the linear transformation step. Comparing the raw data set shown in Figure 1 column 1 with the interpolated data shown in column 3, we see that we were able to obtain a profile of heterogeneity in all heart points that corresponded well with the clinical data, but was spatially smooth. We chose to use this smoothed representation as it provided a robust general description of heterogeneity in the heart that helped guard against possible spurious recordings. (Note that the patient 1 dataset we use here is the same as the one used in Figure 4 in [31]).

For dataset 1, a large region of the posterior wall of the left ventricle contained steep restitution slopes, with values close to 3. The right ventricle contains more shallow restitution slopes, with values around 0.5-1. Between these regions, intermediate values were present. The mean +/- SD restitution slope was 1.78 +/- 0.65. Dataset 2 had a relatively small region on the anterior wall with high slope values, whereas the rest of the bulk tissue was characterized by shallow restitution. The mean +/- SD restitution slope was 1.01 +/- 0.48. Both profiles are illustrated in Figure 3, where red areas correspond to steep restitution slopes ($S_{\text{max}} = 2.5 - 3$), whilst blue areas correspond to shallow restitution slopes ($S_{\text{max}} = 0.5 - 1$). Figure 11 illustrates two short-axis slices with maximum restitution slopes that have been interpolated from the epicardium through to the endocardium (for dataset 1).

### Parameters of the cell model

To model cardiac tissue with the desired regional APD restitution properties we fitted parameters of the TNNP model to different maximum restitution slopes. For each computational point of the ventricular geometry, the value of $S_{\text{max}}$ was used to individually assign cell model parameters. To generate restitution curves, we paced a single cell model with a series of 10 S1 stimuli at a BCL of 600 ms, followed by a single S2 stimulus delivered at a specified DI after the last S1 action potential. The restitution curve was generated by decreasing the S1-S2 interval (and hence DI), and plotting the $APD_{50}$ of the S2 action potential versus the preceding DI value. We reproduced a variety of slopes between 0.4 and 3 by varying the parameters $G_{Kr}$, $G_{Ks}$, $G_{pCa}$, $G_{pK}$ and $\tau_f$. Figure 4 shows the values of these parameters used to obtain the given maximum restitution slopes. Note, that for slopes $S_{\text{max}} < 0.4$ we used $S_{\text{max}} = 0.4$, and for slopes $S_{\text{max}} > 3$ we used $S_{\text{max}} = 3$ (grey lines in Figure 4). Figure 5 shows an example of some APD and APD restitution curves for different parameter settings, together with experimental data to which these restitution curves were fitted. More information about fitting of experimental restitution curves using the TNNP model can be found in Ten Tusscher et al. [49].

### Numerical approach

Equations for the gating variables in the TNNP model were integrated using a Rush and Larsen integration scheme [45]. To integrate Equation 1, we used a forward Euler scheme with a time step of $\Delta t = 0.02$ ms and a space step of $\Delta x = 0.25$ mm, and the following Laplacian was evaluated at each point in the human ventricular geometry:

$$\Delta(i, j, k) = \frac{\partial}{\partial x_i} \left( D_{ij} \frac{\partial V_m}{\partial x_j} \right)$$

which can be discretized to the following equation:

$$L(i, j, k) = \sum_{l=0}^{l=18} w_l V_m(l)$$
Figure 1: Distribution of epicardial restitution, $S_{max}$ shown on the polar projection, with the epicardial apex at the center of each plot and the ventricular base at the outer circumference. For the polar projections, the anterior, posterior, LV, and RV portions of the ventricular epicardium are shown at the bottom, top, left, and right, respectively. Top row: dataset 1. Bottom row: dataset 2. Column 1: Simple triangle based linear surface interpolation using Matlab’s GRIDDATA function. Column 2: After diffusion and application of the $3 \times 3 \times 3$ moving average window. Column 3: After linear transformation.

Figure 2: Correlation plots of clinical $S_{max}$ values versus model $S_{max}$ values after diffusion and moving average window procedures. Left: dataset 1. Right: dataset 2.
Figure 3: 3D plots of restitution $S_{max}$. Top row: dataset 1. Bottom row: dataset 2. From left to right: LV, RV, anterior and posterior views.

where $l$ is an index running over the 18 neighbors of the point $(i,j,k)$ and the point itself, and $w_l$ are the weights defined for each neighbor point containing information about the voltage contributed to the Laplacian at each point $(i,j,k)$. Weights are calculated at each point using the local conductivity tensors calculated by Equation 3. To ensure a zero axial current flow from heart points to non-heart points, no flux boundary conditions were imposed by setting weights to zero if a neighbor lay outside the heart geometry.

To initiate 3D scroll waves, we used an S1-S2 protocol, in which the S2 stimulus was activated in the refractory tail of the S1 stimulus, thereby creating a scroll wave. Stimulus currents were applied at twice the diastolic threshold value. For each restitution slope profile, we performed simulations of VT/VF by initiating a scroll wave in the free wall of the left ventricle. Simulations lasted for 8 seconds or were terminated if there was no activity present.

Assuming that the medium is an infinite volume conductor, electrograms can be calculated using the dipole source density of the membrane potential in all voxel points using [37]:

$$ECG = \int_V \frac{D V_m \cdot \hat{r}}{r^3} dV$$

where, $V$ is the domain of integration (i.e., the ventricular volume), and $\hat{r}$ is the vector from each point to the recording electrode, which was placed 10 cm from the center of the ventricles in the anterior direction of the transverse plane.

Scroll wave filaments were detected using an algorithm proposed by Fenton and Karma [13]. If there is a spiral wave in 2D (a scroll wave in 3D) present, the core (filament) can be defined as the point(s) for which the excitation wavefront and waveback meet. This can be calculated as the intersection points of the -60 mV isopotential line and the $dV/dt = 0$ iso-line. Voxel data corresponding to these intersection points were then stored. Individual filaments were detected by iteratively joining neighboring voxels that were designated as filament points. All voxels that belonged to the same filament were assigned a unique identifier. Filaments were determined at 10 ms intervals. Of these filaments, we tracked: the time of birth, time of death, time of bifurcation, time of amalgamation, lifespan, filament from which a filament bifurcated, filament into which a filament amalgamated, and ultimate filament to which a filament can
Figure 4: Model parameters determining the maximum slope of the APD restitution curve. The y-axes are $G_{Kr}$, $G_{Ks}$, $G_{pCa}$, $G_{pK}$ (in nSpF$^{-1}$) and $k_f$, respectively. The parameter $k_f$ is the multiplication factor of $\tau_f$. The x-axis shows the maximum slope of the restitution curve $S_{max}$. Grey lines represent cutoff values (see text for further explanation).
be traced back through the bifurcations events.

All simulations were coded in C++ and MPI and were run on 16 processors of a Beowulf cluster consisting of 16 Dell 650 Precision Workstations (dual Intel Xeon 2.66 GHz). Simulating 1 second of wave propagation in the ventricles took approximately 6.5 hours of wall-clock computation time. Ventricular geometry, wave patterns and scroll wave filaments were visualized using the marching cubes algorithms for isosurface detection in voxel data, and OpenGL for isosurface rendering.

Results

Wavefronts and ECG signal

In the first series of simulations we initiated a spiral in the free wall of the left ventricle using a S1-S2 protocol. In Figure 6, we show snapshots of consecutive wavefronts and the ECG pattern for both patient datasets (dataset 1 in the top row, and dataset 2 in the bottom row). For dataset 1, we observed that the initial spiral broke down into a chaotic fibrillatory pattern, and that the ECG signal was irregular and complex (dominant frequency of 4.6 Hz). For dataset 2, the initial spiral remained stable in the LV. Note that the spiral was not anchored, and did not (hyper)meander nor drift during the entire simulation. The ECG signal was periodic (dominant frequency of 4.5 Hz), which resembles ECG signals during ventricular tachycardia (VT). The frequency spectra of both ECG signals are shown in Figure 7. Although the simulations had similar dominant frequencies, the frequency spectrum of dataset 1 was broader in comparison to that of dataset 2, which had a single dominant peak. These observations are characteristic of the differences between VF and VT, respectively, and the frequencies are similar to those reported in clinical [8, 30, 32, 56] and numerical studies [48].

Number of filaments

A convenient way to quantify the complexity of excitation patterns in the thick walled ventricles of the heart is by determining the number of scroll wave filaments of the excitation sources [48, 51, 44, 42, 21, 7, 10, 34]. A scroll wave filament is a line around which a 3D spiral wave rotates. When such a filament intersects with the surface of the heart, a phase singularity (PS) manifests on the heart surface. For dataset 2, we observed just one reentrant source, represented by a single filament.
Figure 6: Wavefronts (in red on the left) and ECG signals (right). Top: dataset 1. Bottom: dataset 2. The first snapshot shows the spiral after initiation on the left ventricular free wall and the second snapshot shows wavefronts after 5 seconds of simulation time.

Figure 7: Frequency spectra of ECG signals. Black: dataset 1. Red: dataset 2.
In Figure 8, we show a snapshot of the filaments present for dataset 1 after 5 seconds of simulation time. Here the excitation pattern was organized by approximately 15 filaments. Most of these filaments extended from the epicardium to the endocardium, with only 5 filaments located entirely within the myocardial walls. We observed that the majority of filaments were located near the base of the heart, whereas very few filaments were present near the apex. Furthermore, most filaments were present in the left ventricular wall, i.e., the region with high restitution slope values. The filament numbers and shapes fluctuated during the course of the simulation. In Figure 8, we show the time dynamics of the number of filaments during 8 seconds of simulation. After an initial phase of growth, the number of filaments fluctuated around 12-20. The average number of filaments was 14.9, which is within the range reported by Ten Tusscher et al. [48]. We also show the number of PS visible on the epicardium. The average number of PS was 10.7, thus the ratio of the number of filaments to PS was approximately 1.4, consistent with [48].

We analyzed how filaments were created and destroyed over time through death, birth, bifurcation and amalgamation events. This is shown in Figure 9 for dataset 1. Horizontal lines indicate individual filaments and their lifespan. The start of a line is determined by the birth of a filament or the bifurcation from another filament. The end of the line occurs when the filaments disappear, i.e., the death or the amalgamation of a filament with another filament. Short horizontal lines in Figure 9 correspond to short living filaments, and long lines correspond to long living filaments. During the simulation we detected 1463 filaments and 379 births, 547 deaths, 1085 bifurcations and 917 amalgamation events. In figure 9 we can see that most of the filaments exist only for a short periods of time, although there are small number of long lived filaments.

Role of tissue heterogeneity

To determine the effect of tissue heterogeneity on wave patterns during VF we performed a series of simulations in which we varied the degree of APD restitution heterogeneity in the heart. We did this by using the following linear transformation:

\[ S_{\text{new}} = S_{\text{avg}} + \epsilon(S_{\text{max}} - S_{\text{avg}}) \]  \( (9) \)

where, \( S_{\text{new}} \) is the new value of the maximum restitution slope at each given point, the average maximum slope taken over all points of dataset 1 is \( S_{\text{avg}} = 1.78 \), \( \epsilon \) is a variable that scales the degree of heterogeneity and \( S_{\text{max}} \) is the original value of the maximum restitution slope at each given point for dataset 1. Clearly, \( \epsilon = 1 \) corresponds to the fully heterogeneous simulation of dataset 1 (presented above), \( \epsilon = 0 \) corresponds to a spatially homogeneous restitution model with a slope of 1.78, and intermediate values of \( \epsilon \) scale the degree of heterogeneity: larger values of \( \epsilon \) correspond to more heterogeneous properties.
Figure 9: Filament history for simulated VF. Horizontal lines correspond to individual filaments and start at the time a filament appears (through birth or bifurcation) and stop at the time a filament disappears (through death or amalgamation). Filaments get assigned unique identity numbers that are not reused once a filament has died. Different colors are used to indicate clusters of filaments that can be traced back through bifurcation events to the same initial filament, which is the first filament of that color. We use different colors for filaments with the same ancestor only if the filament cluster has a size of 5 or more filaments. All other filaments that either have arisen through birth rather than bifurcation, or belong to a small cluster are colored black.
We performed a series of computations similar to that shown in Figure 6. The spiral was initiated in the LV wall using a S1-S2 protocol. We used $\epsilon$ values of 0, 0.25, 0.5, 0.75 and 1. The duration of all simulations was 8 seconds. We investigated the maximum number of filaments, average number of filaments, maximum number of epicardial PS and average number of epicardial PS for each simulation. The results are shown in Figure 10 and we see that for $\epsilon = 0$ (homogeneous setting) full blown breakup did not occur for the given slope (1.78). We found that to induce breakup for our heart model, we needed to increase the restitution slope to above 1.8 (results not shown). This is consistent with the slope value reported by Ten Tusscher et al. [49], given the difference in the methods used for slope determination (see methods section). We see that the maximum number of filaments and the average number of filaments increased for increasing heterogeneity. Similar results were found for the epicardial PS.

![Figure 10: Number of filaments and epicardial phase singularities (PS) for different degrees of APD restitution heterogeneity ($\epsilon = 0$, homogeneous; $\epsilon = 1$, heterogeneous).](image)

To understand the mechanism of increased filament numbers with increasing heterogeneity, we investigated filament locations in the heart. Figure 11 shows all the locations of filament voxels across two slices of the heart together with the maximum restitution slopes (for the 8 second run with $\epsilon = 1$). The majority of the filaments were located in regions containing steep restitution slopes, and they were evenly distributed across these steep slope regions. Indeed, the mean +/- SD restitution slope taken across all voxels traversed by the filaments was significantly steeper (2.17 +/- 0.55) than that for the voxels spanning the remainder of the model (1.76 +/- 0.65, $p < 0.005$, 2-tailed Student t-test).

In our model, the slope of the restitution curve is related to APD (see Figure 5) and thus gradients in restitution slopes are associated with gradients in APD. Such APD heterogeneities could potentially induce new wave breaks by themselves (even without steep restitution) and this would be expected to occur in areas of abrupt APD variation. However, we did not observe this in our simulations. We observed comparatively fewer numbers of filaments in regions containing restitution slope gradients. Thus the increase in complexity of VF is more likely to be directly due to the increase in size of regions with a steep enough restitution slope ($> 1.80$), rather than an increased occurrence of new breaks at larger gradients of heterogeneities in APD.

An additional fact in favor of this hypothesis is that the electrical turbulence induced by steep restitution would be expected to be homogeneously distributed across entire regions of steep restitution, and this is what we have observed (Figure 11).

We finally investigated the spatial-temporal distribution of excitation periods for all voxels in the 3D ventricular anatomy for different extents of heterogeneity ($\epsilon$). For this, we determined excitation periods in every voxel after 2 seconds of transient processes using a 2 second window. Figure 12 shows the distribution of excitation periods on the epicardium, averaged in a time interval between 2-4 seconds for $\epsilon = 1$. We see that there are several distinct regions with different excitation frequencies. We followed
Figure 11: Location of filament voxels (black) for the entire 8 seconds run. Illustrated are short-axis slices mid-way between base-to-apex (left), and one-third of the distance from the base-to-apex (right). Maximum restitution slopes are represented using a pseudo-color spectrum.

We compared the spatial distribution of excitation periods in the interval 2-4 seconds for all values of $\epsilon$. For the homogeneous simulation ($\epsilon = 0$), we found that the average period values were distributed homogeneously and did not change over time. For $\epsilon$ values between 0 and 1 we found that the number of regions with different periods increased as the heterogeneity ($\epsilon$) in APD slopes increased.

To quantify this increased heterogeneity in excitation period regions, we determined the average period value (dots) and the 95% confidence interval period values (bars) for different values of $\epsilon$ (see Figure 13). We did this both for excitation periods distributions across the entire ventricular mass (grey) and for distributions across the ventricular epicardium (red). Comparing the grey and red bars, we see that the period distributions on the epicardial surface were similar to those measured over the entire ventricular mass. We see that the average periods (grey and red dots, respectively) remained approximately equal for all values of $\epsilon$, but that the width of the period distributions increased with increased $\epsilon$ (grey and red bars, respectively).

Given the observed temporal variations in excitation period domains and our results on filament...
locations, we conclude that the increase in complexity of excitation period patterns is primarily caused by the increased number of filaments under increased heterogeneity rather than the increased heterogeneity in anatomically defined APD restitution regions itself.

Figure 13: 95% confidence interval period values. Grey bars: minimum and maximum periods found in 95% confidence interval period values for all voxels in the entire ventricular anatomy. Red bars: minimum and maximum period found in 95% confidence interval period values only for the 256 electrode positions on the epicardial surface.

Discussion

We have used a detailed human ventricular model to study wave organization during VF in the presence of APD restitution heterogeneity. The model contains a detailed description of human ventricular anatomy, fiber direction anisotropy, and the electrophysiological behavior of human ventricular cells. Recent clinical studies by Nash et al. [31] provided APD restitution properties at 256 locations spanning the entire ventricular epicardium for different patients. This study showed that APD restitution slopes are organized into different regions with slopes ranging from 0 to well over 3.

We incorporated the clinical data of Nash et al. [31] into our anatomically realistic model of the human ventricles by mapping from the 256 electrode locations to our ventricular geometry and interpolating the projected data using a diffusion based algorithm. Restitution slopes were then fitted by tuning selected parameters of the TNNP model, which were individually specified at each voxel based on the interpolated restitution slopes. For this study, we used datasets of 2 patients: dataset 1 contained regions of shallow and steep restitution slopes, while dataset 2 contained mostly shallow restitution slopes. Thus, the heterogeneity profiles of both datasets were different.

Heterogeneities are not necessary to induce VF in the human heart. As reported by Ten Tusscher et al. [48] VF can occur in a homogeneous heart if the slope of the restitution curve is higher than 1.5. In our model, a slope value of 1.8 or higher is necessary to induce VF. This difference in slope value is due to the difference in slope determination method used between Ten Tusscher et al. [48] and this paper (see methods). Note, that the minimum slope value necessary to induce VF in a homogeneous heart is substantially higher than the value of 1, predicted from the original restitution hypothesis. As shown by Cherry and Fenton [5] in a Fenton-Karma model [13] and by Ten Tusscher et al. [49] in the TNNP model, this higher slope value can be explained by electrotonic interactions and CV restitution properties influencing APD alternans.

We analyzed the dynamics of filaments during VF, the formation via birth and bifurcations and the disappearance via death and amalgamation, and the duration of their lifespan. We found that most
rotors were short lived, whereas only a small number of long lived rotors were present during VF. This is in agreement with the findings of [48] and experimental observations on epicardially manifested rotors in animal hearts [44, 43, 21].

We found that APD restitution heterogeneity is not only important for the initiation of wavebreak and re-entry [6, 9], but also affects the number of filaments during VF. We found that an increased level of APD restitution slope heterogeneity leads to more filaments and a broader and more dynamical distribution of excitation periods. We conclude that there is an interplay between the dynamical organization and complexity of VF, and the underlying APD restitution heterogeneity. Furthermore, our results are consistent with the notion that the increase in wave breaks caused by increasing heterogeneity (ε) is predominantly due to the presence of larger areas with steep restitution slope, rather than increased gradients in restitution slope or APD. However, we do not exclude that other factors such as geometric effects, anisotropy or more pronounced APD gradients potentially play a role in wave break formation.

Finally, we found that the number of epicardial PSs correlated well with the total number of filaments, and that distribution of epicardial excitation periods, provides a good estimate of the period distribution within the entire ventricular mass.

Limitations
Clinical data were only available for the epicardial surface of the ventricles. There was no information on restitution properties in the mid-myocardium nor endocardium. To overcome this, the epicardial restitution slope data was extrapolated across the entire ventricular walls using a diffusion based algorithm. Note that a variety of interpolation schemes could have been used to achieve a similar degree of variation. The use of different parameters in our diffusion algorithm may lead to different gradients in slope values for the same set of clinical data. It remains to be investigated how these different heterogeneity profiles with different slope gradients affect the results presented in this study.

Other heterogeneities such as epi-, endocardial and M-cells, Purkinje fibers, laminar sheets and disease conditions (such as fibrosis and gap junction remodeling) were not taken into account in our model and may also contribute to the complexity of excitation patterns during VF.

It should be noted that the mapping of the TNNP model parameters to the restitution slope values that we used is not unique, and that the same slopes may likely be obtained using other combinations of parameter settings. However, we believe that this non-uniqueness should not qualitatively affect the results of our study, as it is the slope of the restitution curve that is the main determinant of the instabilities in our model.

Another limitation is that TNNP model used in our study does not reproduce calcium driven alternans [38, 46, 47], which is an additional source of instability that can lead to VF.

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